

# Blood-vessels' lumen geometric modeling and quantification in 3D images

*Andrzej Materka and Jakub Jurek*  
*Politechnika Łódzka, Instytut Elektroniki*  
[materka.p.lodz.pl/dydaktyka.html](http://materka.p.lodz.pl/dydaktyka.html)



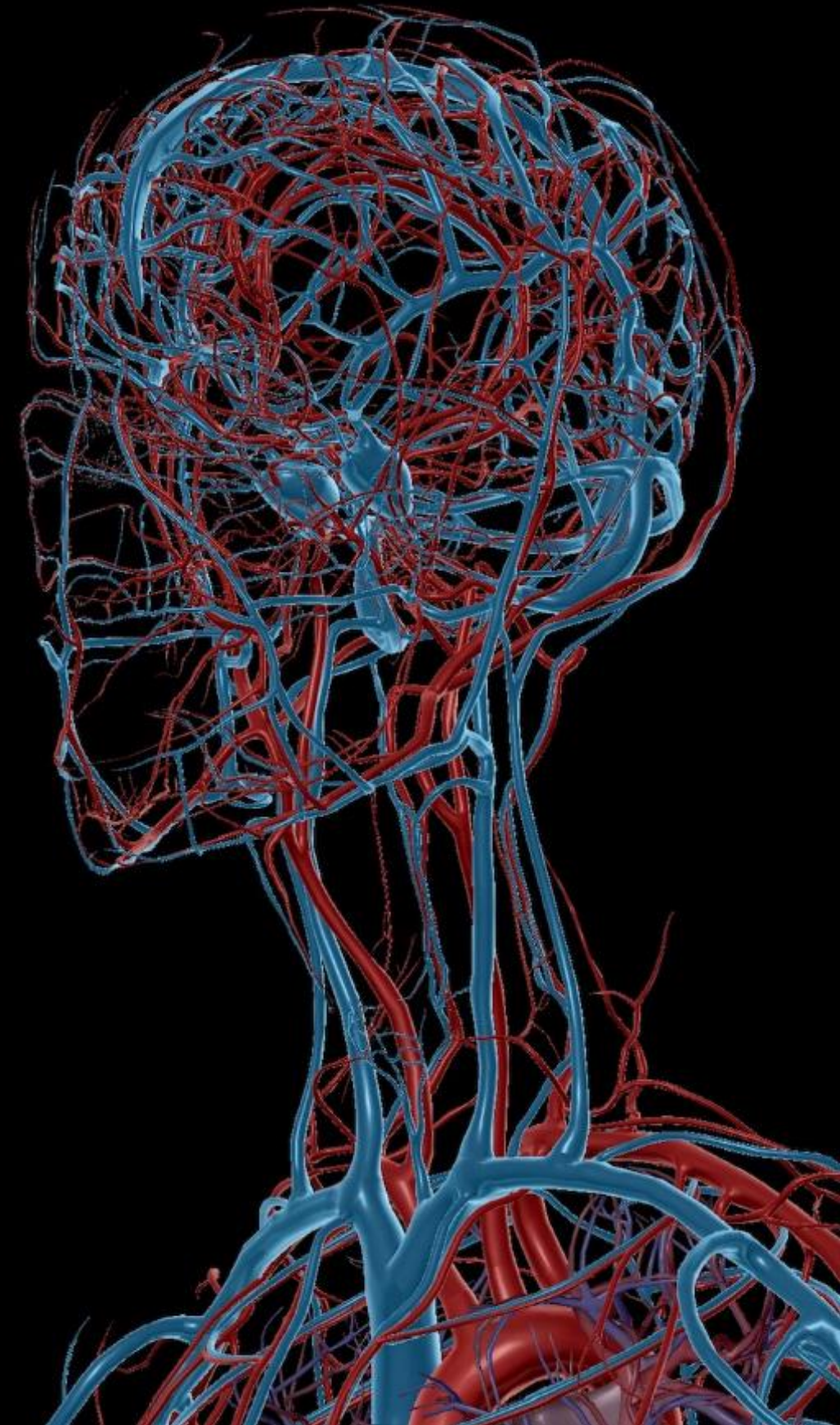
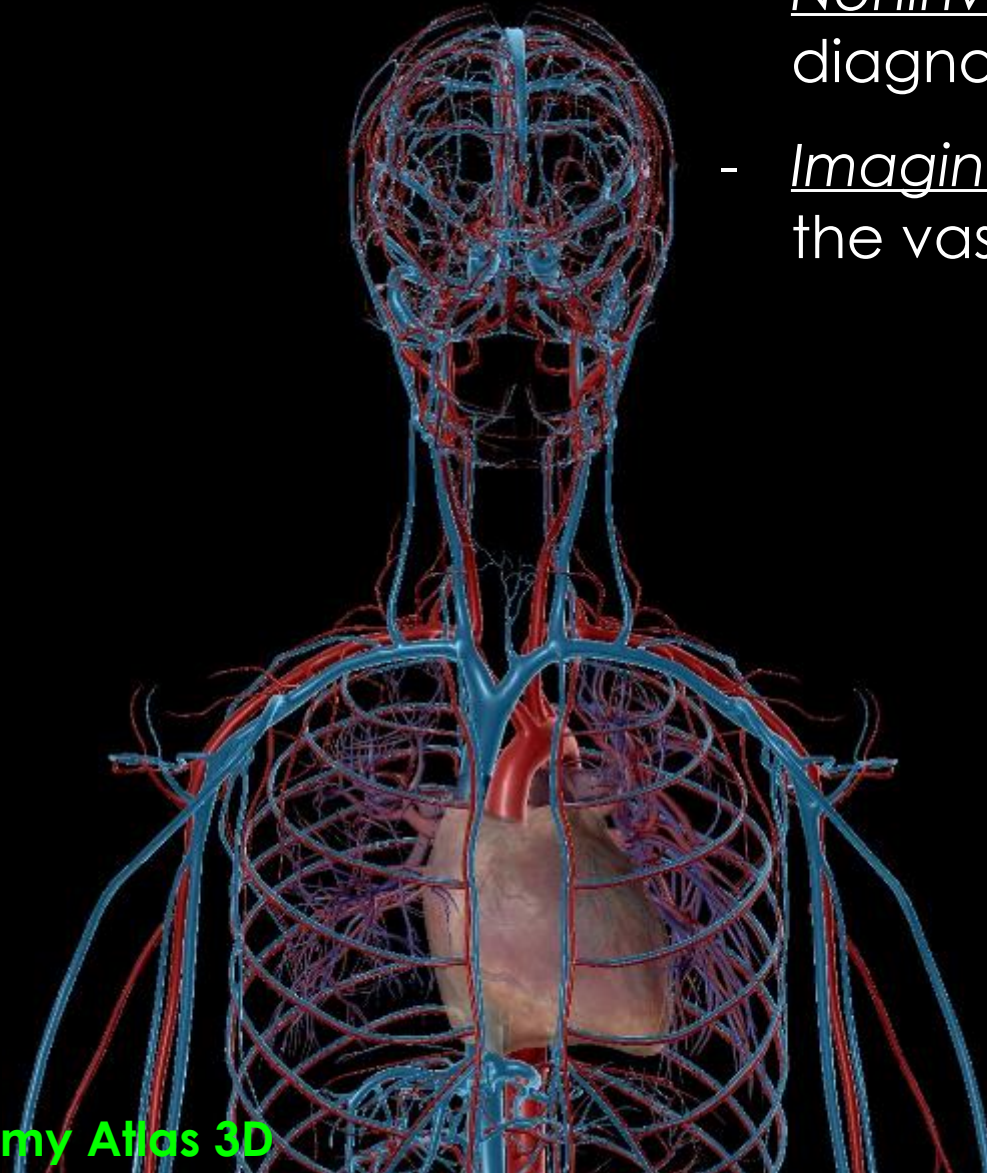
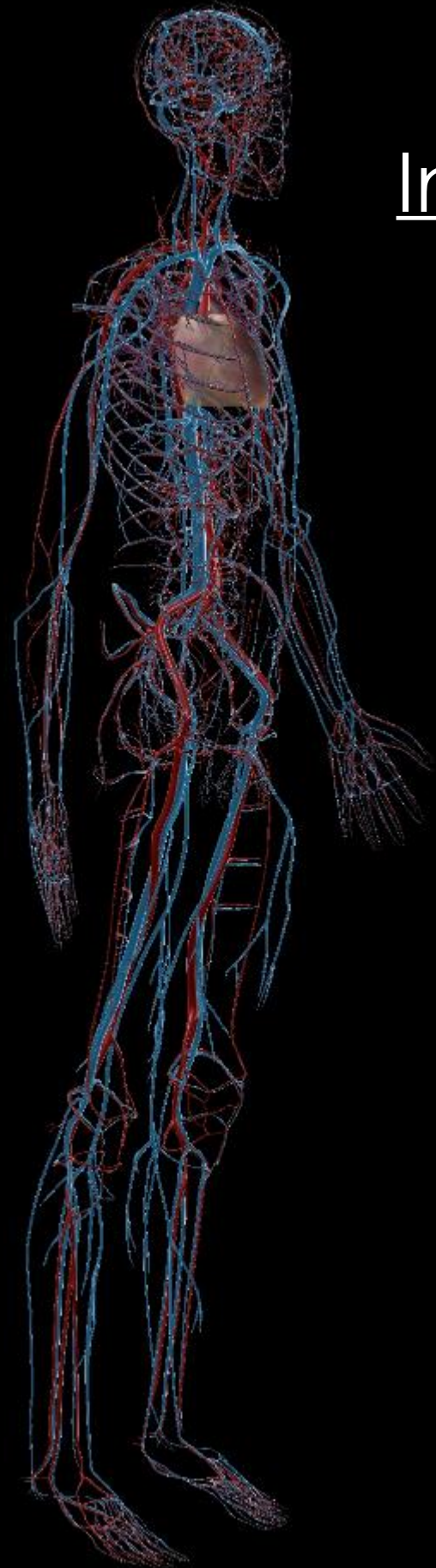
# Overview

- Introduction
- Problem to solve
- Challenges
- Methods
- Examples
- Summary



## Introduction

- Cardiovascular diseases are the leading cause of death worldwide [1].
- They originate mainly from blocked or excessive blood supply to tissues.
- Noninvasive, objective and accurate diagnostic techniques are searched for.
- Imaging techniques play a major role in the vascularity evaluation.





# Introduction



Computed tomography angiography (CTA)

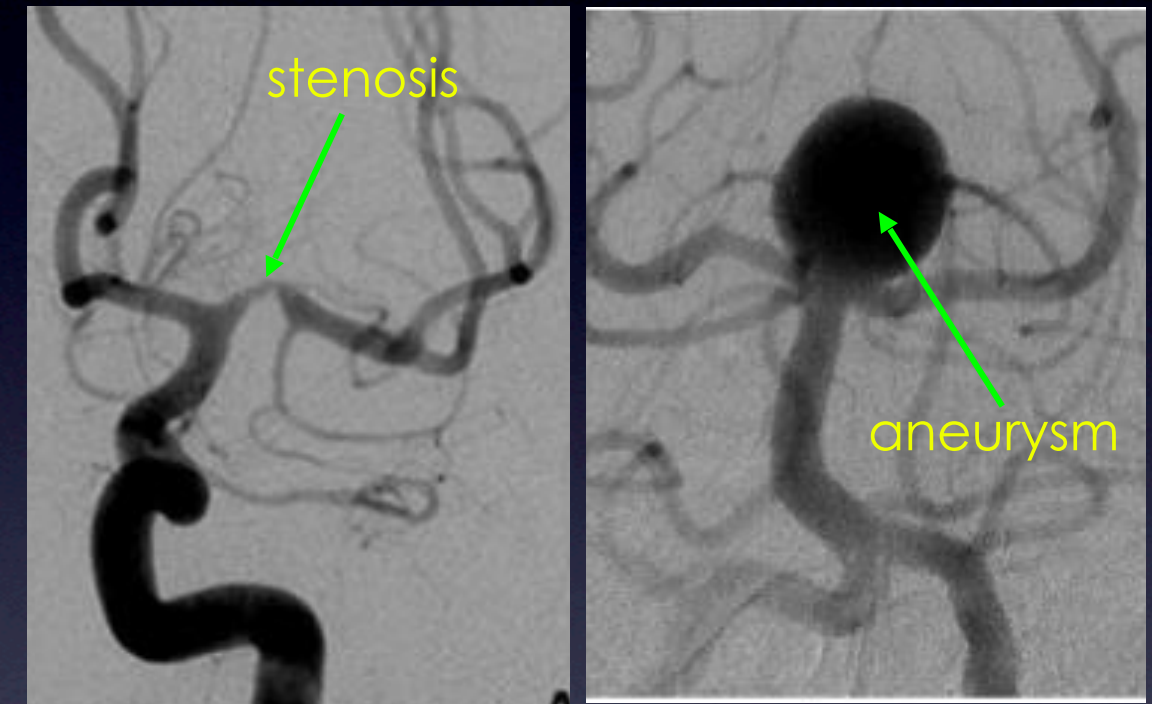
## Medical imaging



Magnetic resonance angiography (MRA)

### Personalized quantification of

- lumen centerline course,
- cross-section shape,
- deformations:





## Problem to solve

Lumen geometry reconstruction  
of blood vessel trees  
given their 3D discrete image

### Geometric model

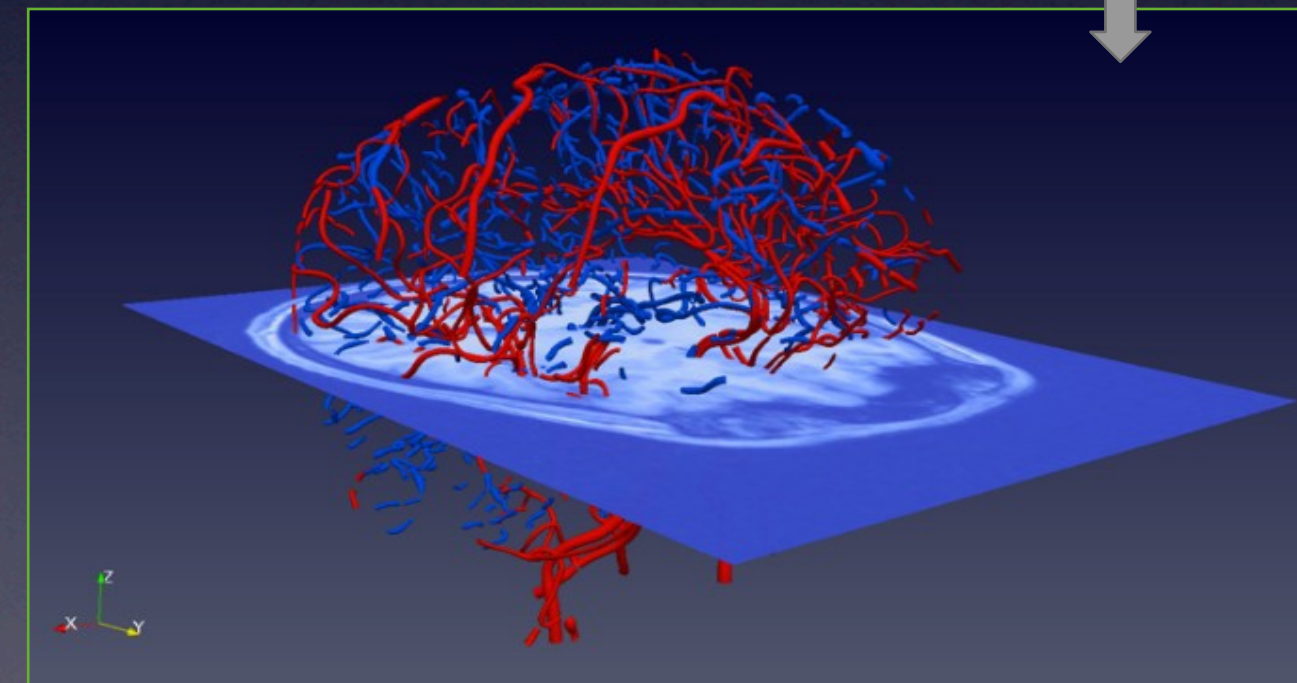
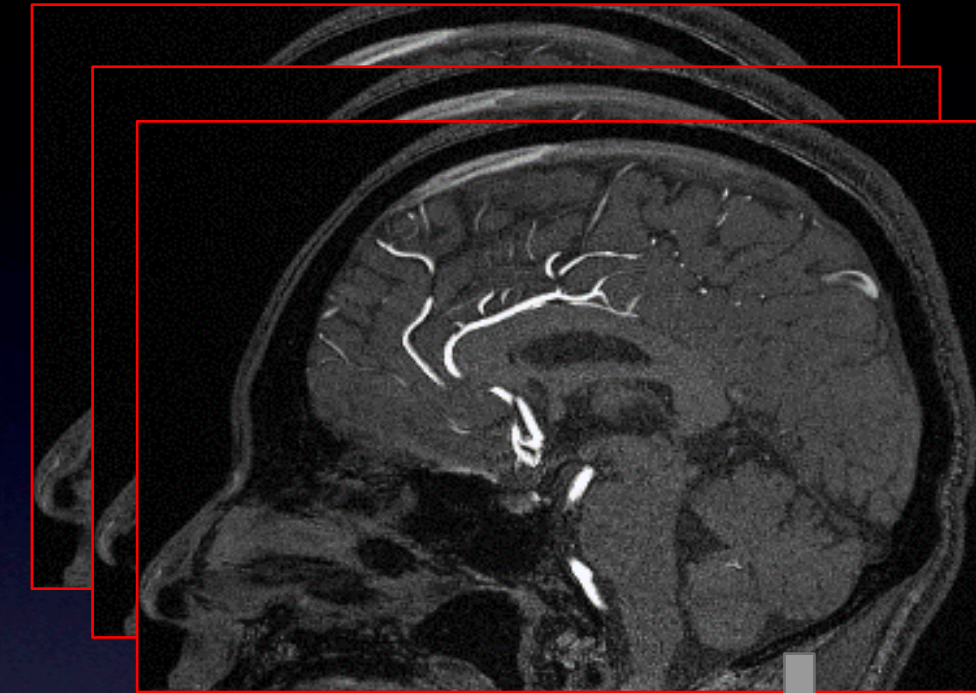
- curved tubes (between n-furcations)
- circular/non-circular cross-sections,
- the diameter varies along the centerline

### Basis for

- diagnostic quantification,
- blood-flow simulation,
- surgery planning/execution,
- education, ...

### Example

Human brain arteries in ToF MRI

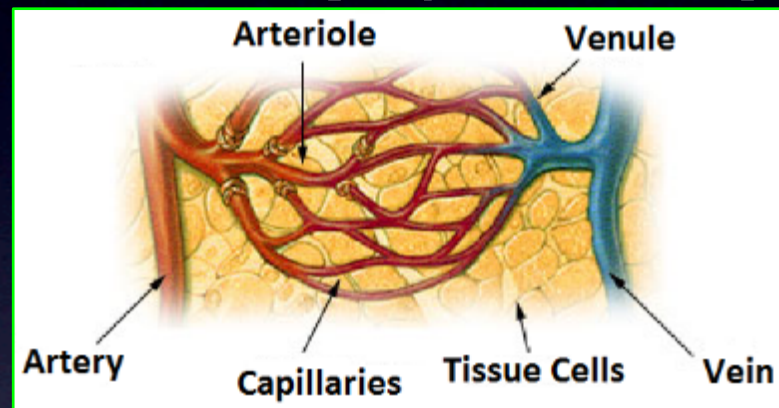




# Challenges

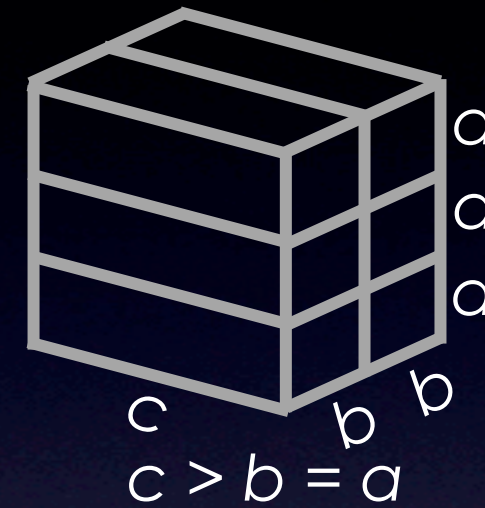
## The scales

$\min\{a,b\} \approx 300 \mu\text{m}$   
 $D \in [10 \mu\text{m}, 40 \text{mm}]$

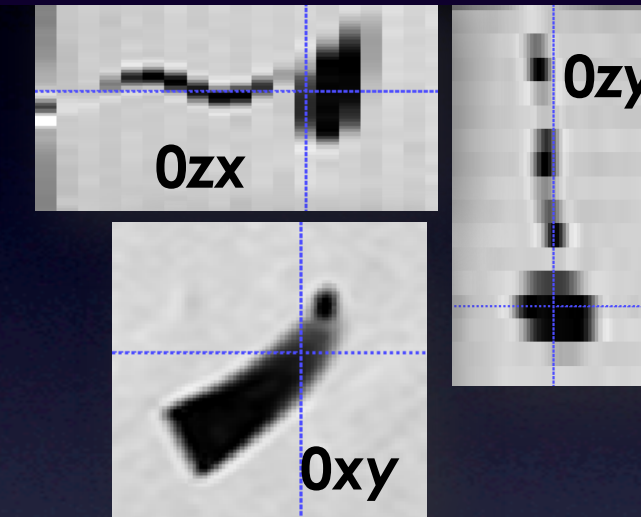


Nieznany autor, licencja: [CC BY-NC](https://creativecommons.org/licenses/by-nc/4.0/)

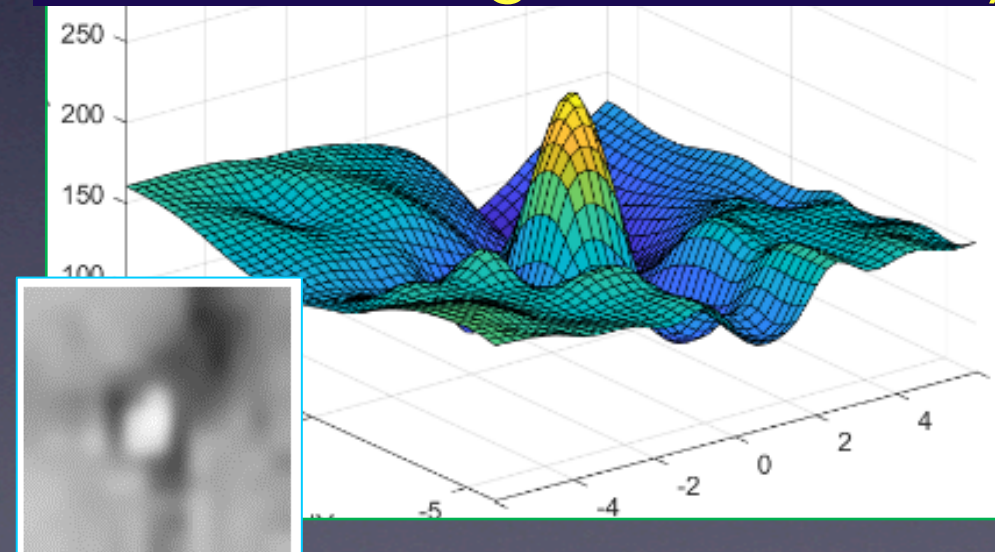
## Discretization, voxel anisotropy



T2w MRI, coronal thick-plane  
 $0.33\text{mm} \times 0.33\text{mm} \times 2.2\text{mm}$

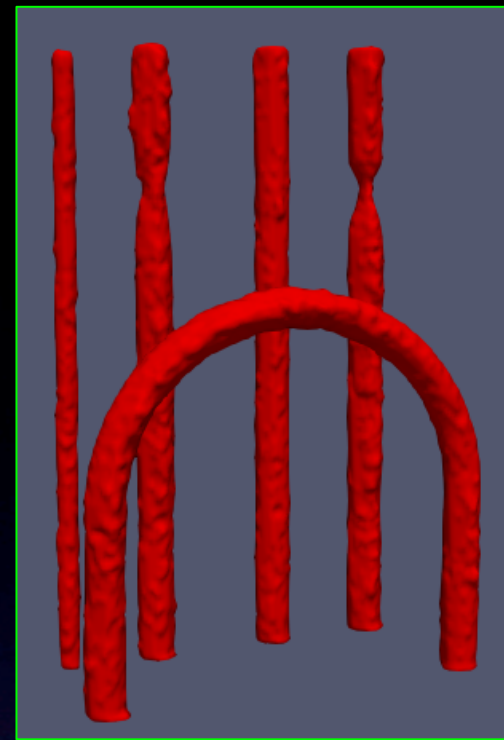


## Uneven background intensity



Noise (SNR)



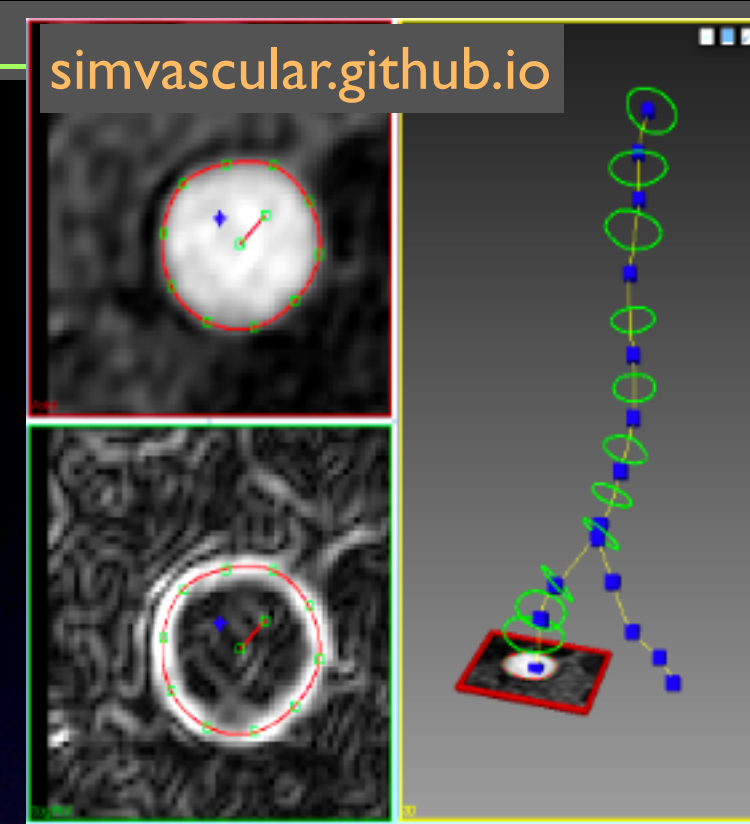


## Modeling of vascular structures in 3D images

Two main approaches [2,3,5,6]

3D lumen binary segmentation

2D cross-section analysis along approximated centerline



- ✗ loss of information due to binarization [9]
- ✗ voxelized surface needs further smoothing

- ✓ no intermediate binary segmentation
- ✓ incorporation of a *priori* knowledge, for robustness [2]

## Methods and algorithms

- Level-set techniques [7]
- ✗ long-lasting computations
- CNNs [8]
- ✗ need for annotated data

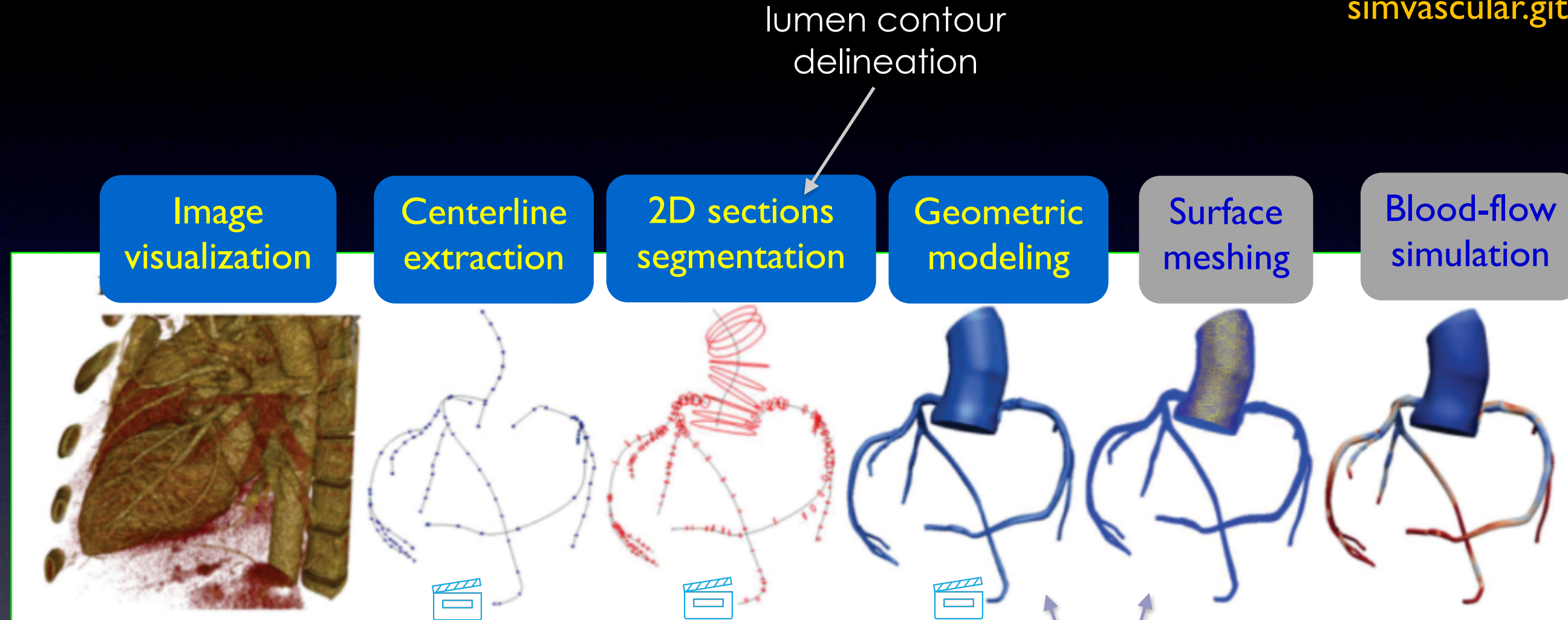
- Image model fitting [9,17]
- ✓ subpixel accuracy
- ✗ computationally demanding, local minima
- CNN-based parameter estimation [21]
- ✓ subpixel accuracy
- ✓ robustness to background elements
- ✓ very short recall time
- ✓ can be trained on synthetic images



# Centerline-based interactive pipeline [22]



[simvascular.github.io/](https://simvascular.github.io/)



↑  
. DICOM  
. Nifti  
. ....

<https://www.pre-scient.com/knowledge-center/geometric-modelling/geometric-modeling.html>

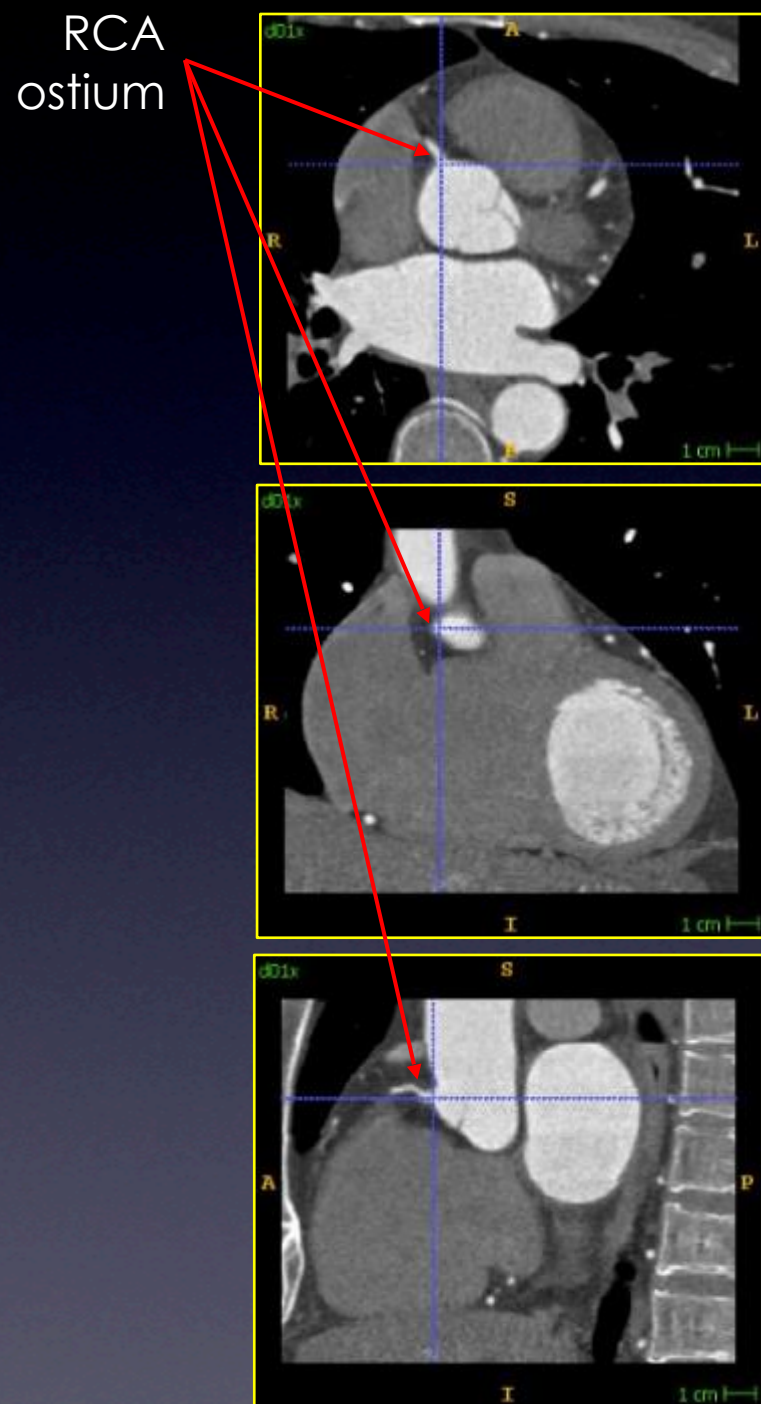
[https://community.cadence.com/cadence\\_blogs\\_8/b/cfd/posts/hurdling-geometry-model-challenges-for-cfd-mesh-generation](https://community.cadence.com/cadence_blogs_8/b/cfd/posts/hurdling-geometry-model-challenges-for-cfd-mesh-generation)



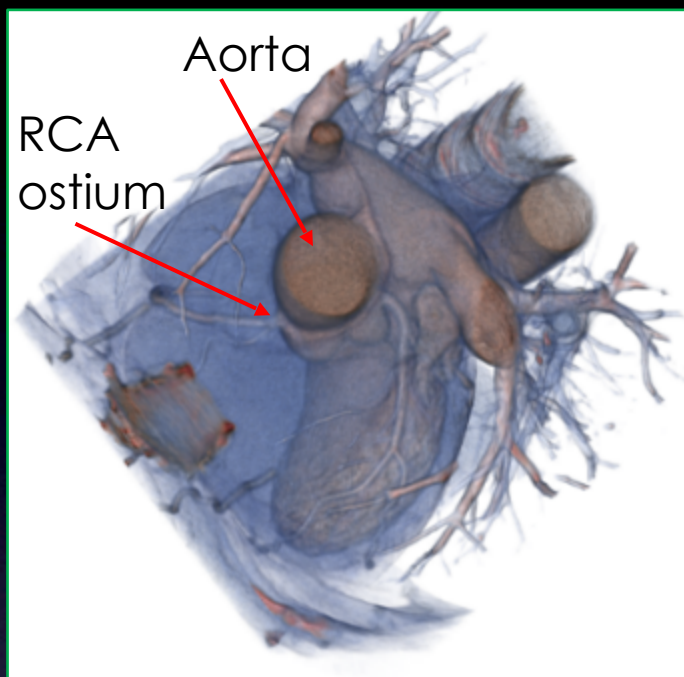
# Centerline-based automated pipeline [9,21]

## Coronary arteries

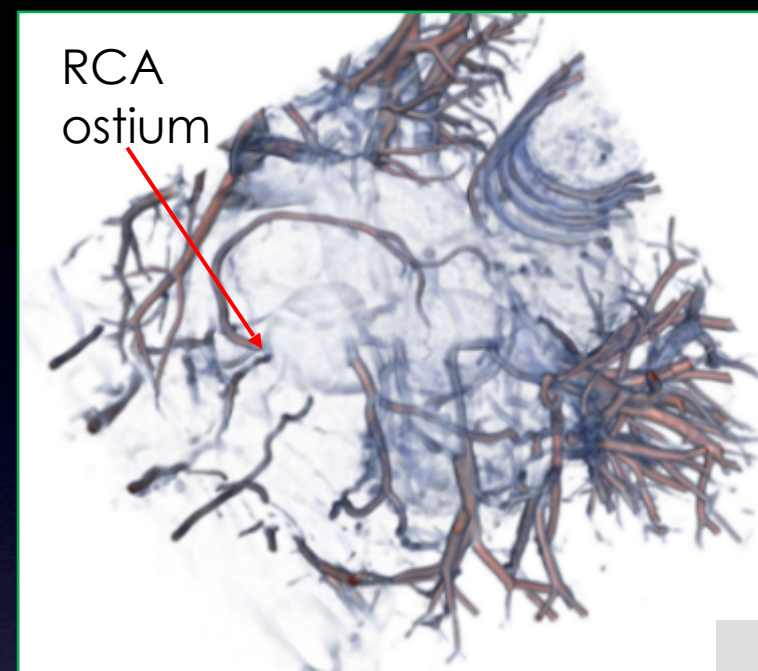
Contrast-enhanced CT [4]



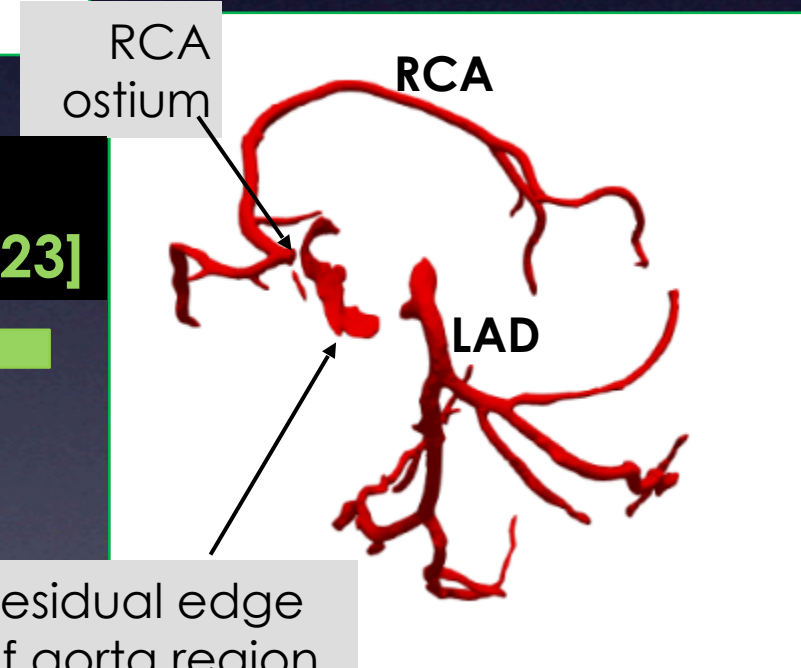
3D image resampling on cross-section planes



Vesselness filtering [10,15,16]

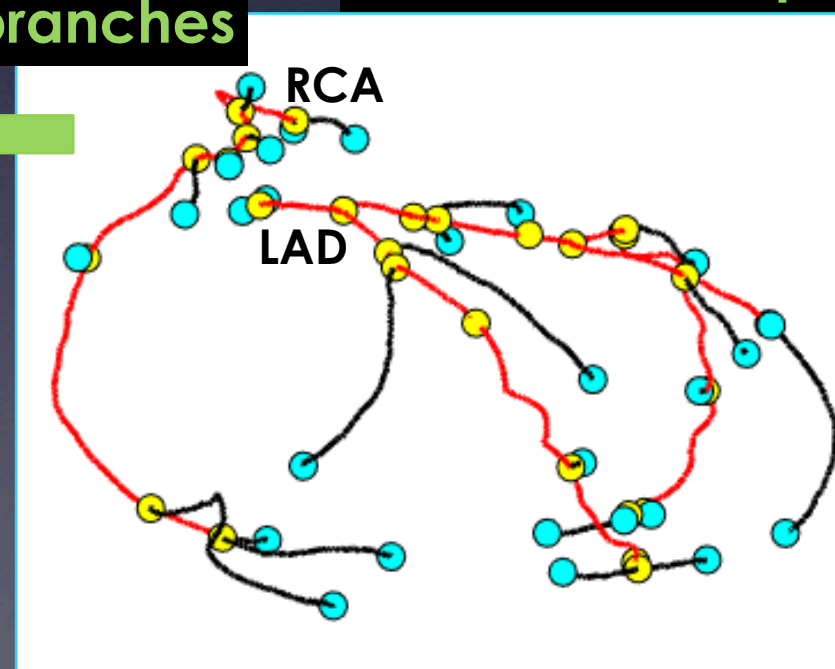
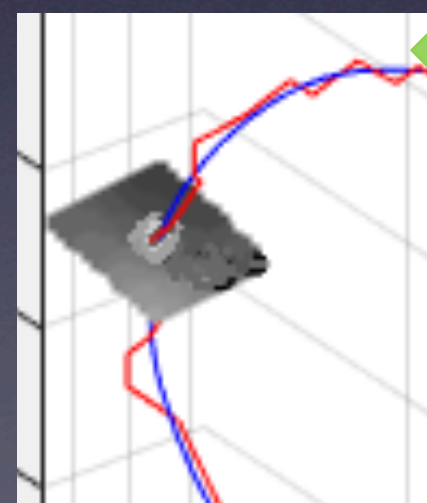


3D region-growing



- 3D binary thinning, - skeleton tree parsing [23]

Smooth approximation of binary skeleton branches



RCA - right coronary artery  
LAD - left anterior descending



# Methods

Image formation model [9,21]

- Scanner assumed to be a linear space-invariant system

$$F(x, y) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(u, v)h(x - u, y - v) dvdu \tag{1}$$

where  $f(x, y; a, b, R, d_x, d_y)$  is the lumen intensity distribution  
 $h(x, y; w)$  is an isotropic Gaussian impulse response.

## Model parameters

- $a$  : background intensity
- $b$  : intensity step
- $R$  : lumen radius
- $w$  : 2D Gaussian blur
- $d_x, d_y$  : centerline shift

- 2D cross-section intensity at a point  $(i, j)$

$$I(i, j; \theta; \sigma) = a + bF(R, w, i\Delta_s - d_x, j\Delta_s - d_y) + \epsilon(\sigma) \tag{2}$$

where  $\Delta_s$  is the sampling interval.

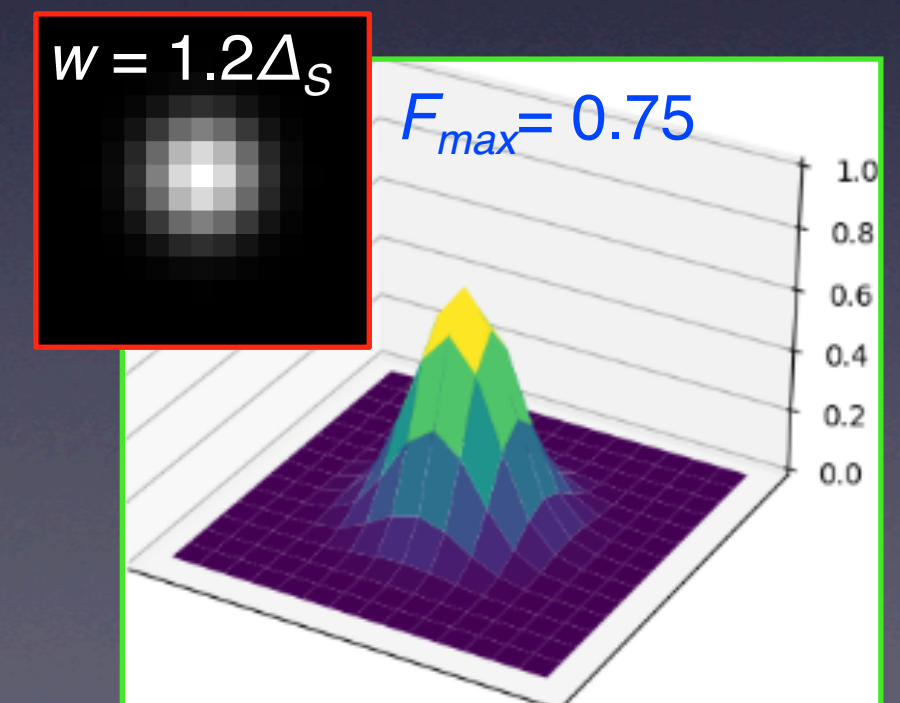
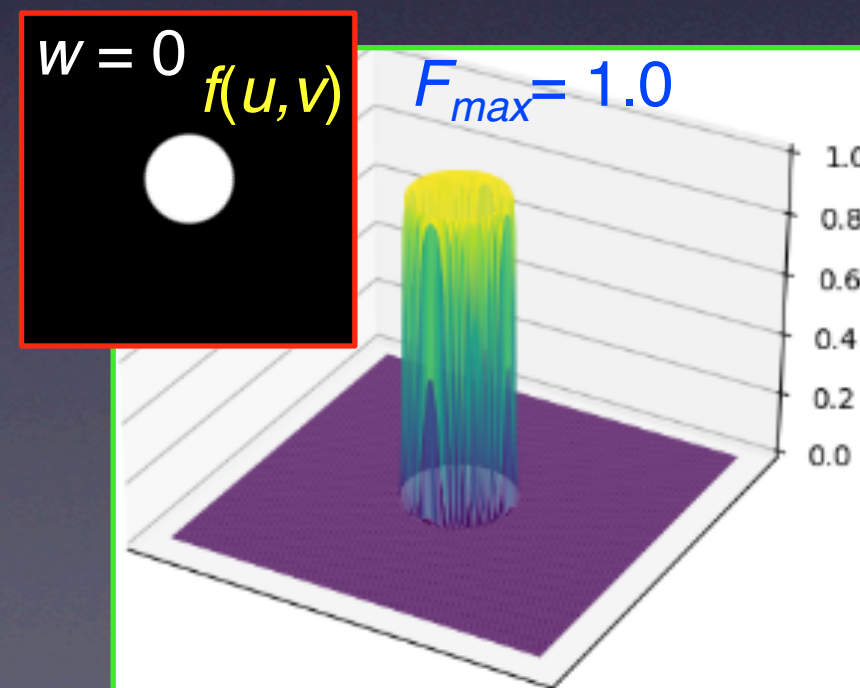
## Random noise $\epsilon$

- zero mean
- standard deviation  $\sigma$

## Parameter vector

$$\theta = (a, b, R, w, d_x, d_y)$$

$R = 2.0\Delta_s$   
 $a = 0$   
 $b = 1$   
 $d_x = 0$   
 $d_y = 0$





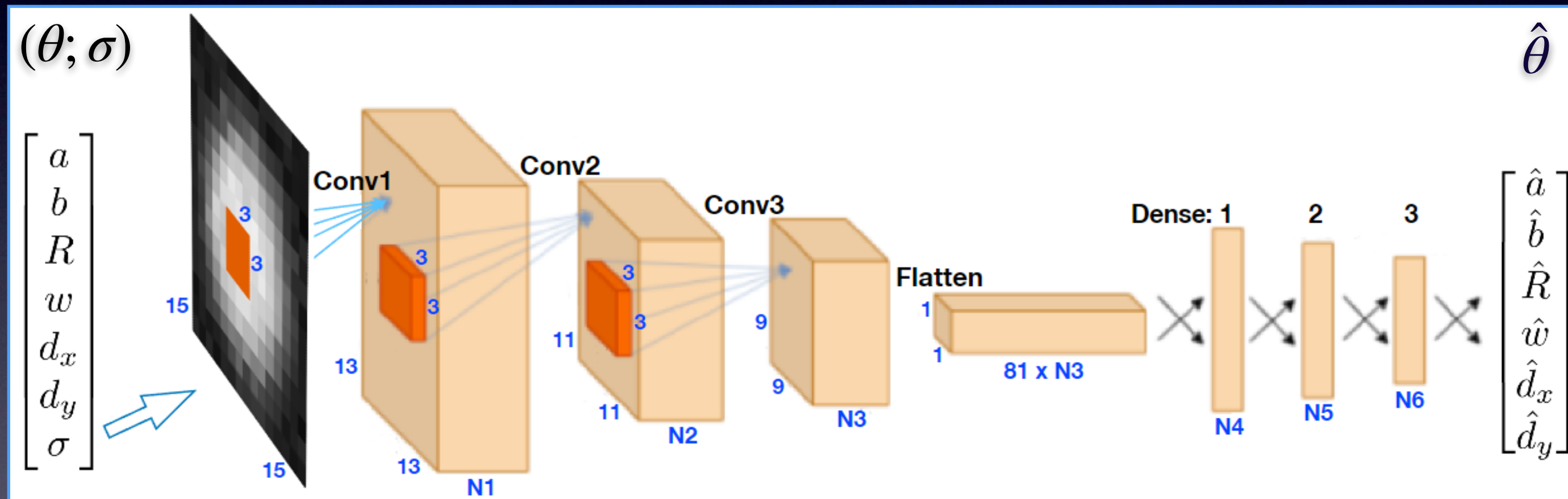
# CNN-based lumen parameters estimation [21,13]

## Transfer learning

A set of 2D images is computed

$$I_m = I(m, \theta_m, \sigma), \quad m \in \{1, \dots, M\}$$

for known model parameters  $\theta_m$  and noise standard deviation  $\sigma$ .

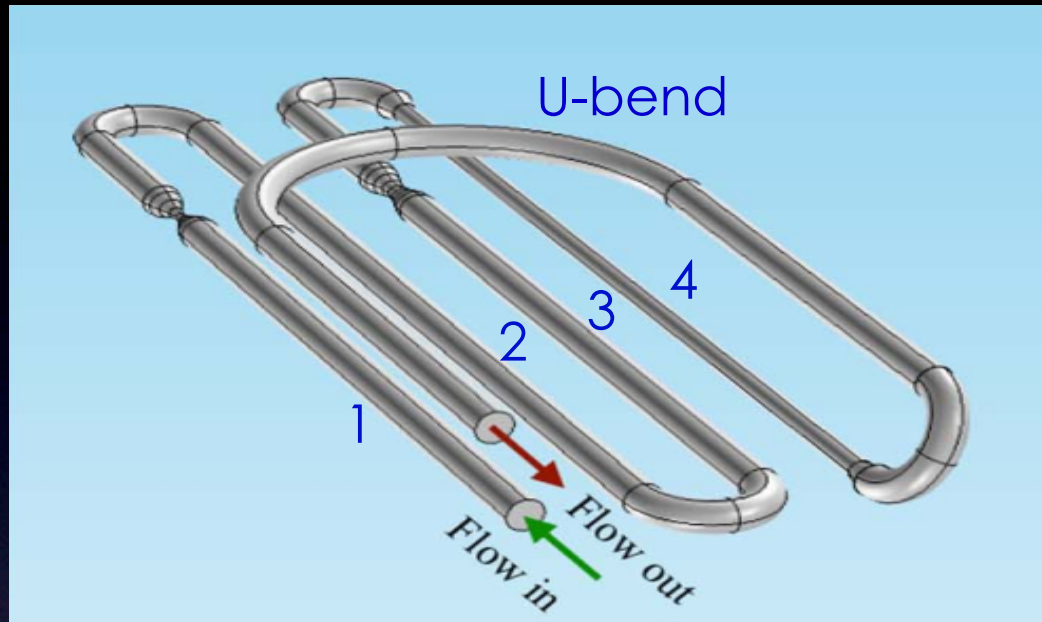


$N1, \dots, N6$  - channels count

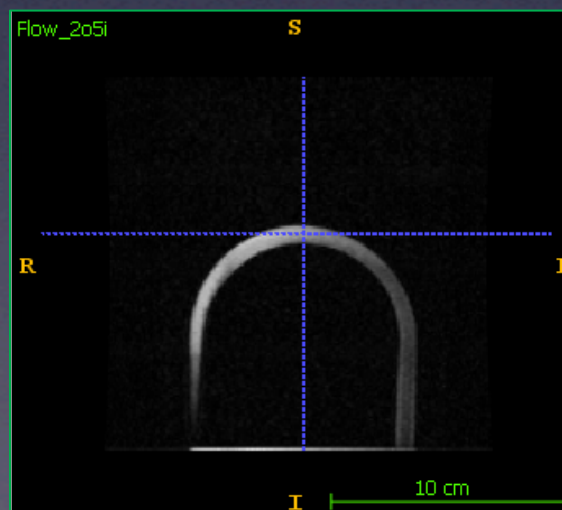
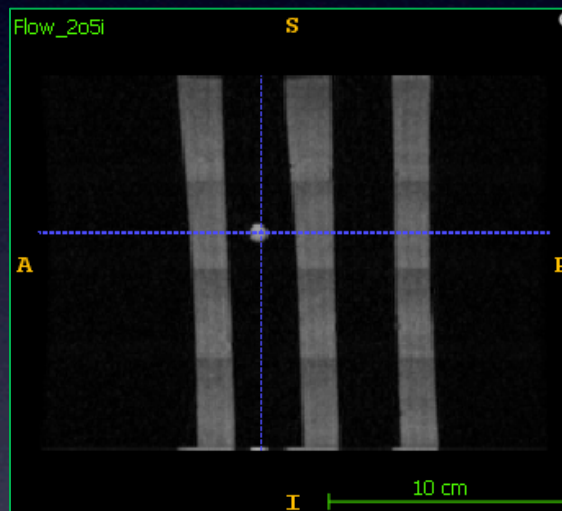
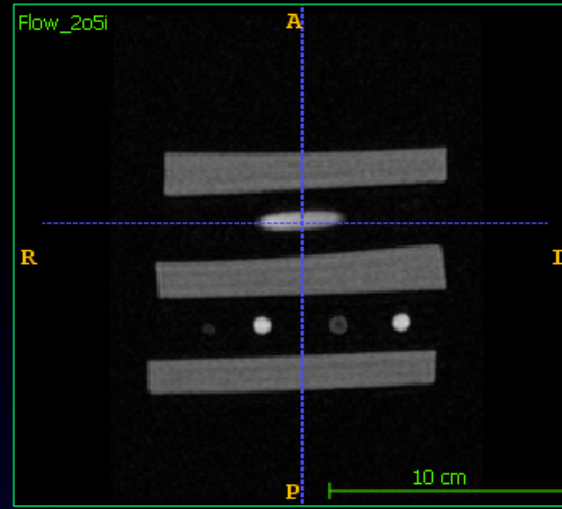


# Example 1

Blood-flow phantom 3D ToF MRI [14]

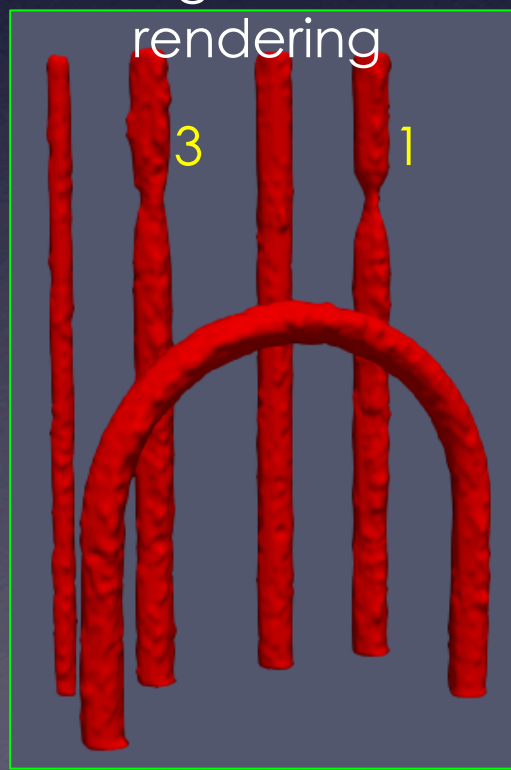


U-bend pipe inner radius: 4 mm

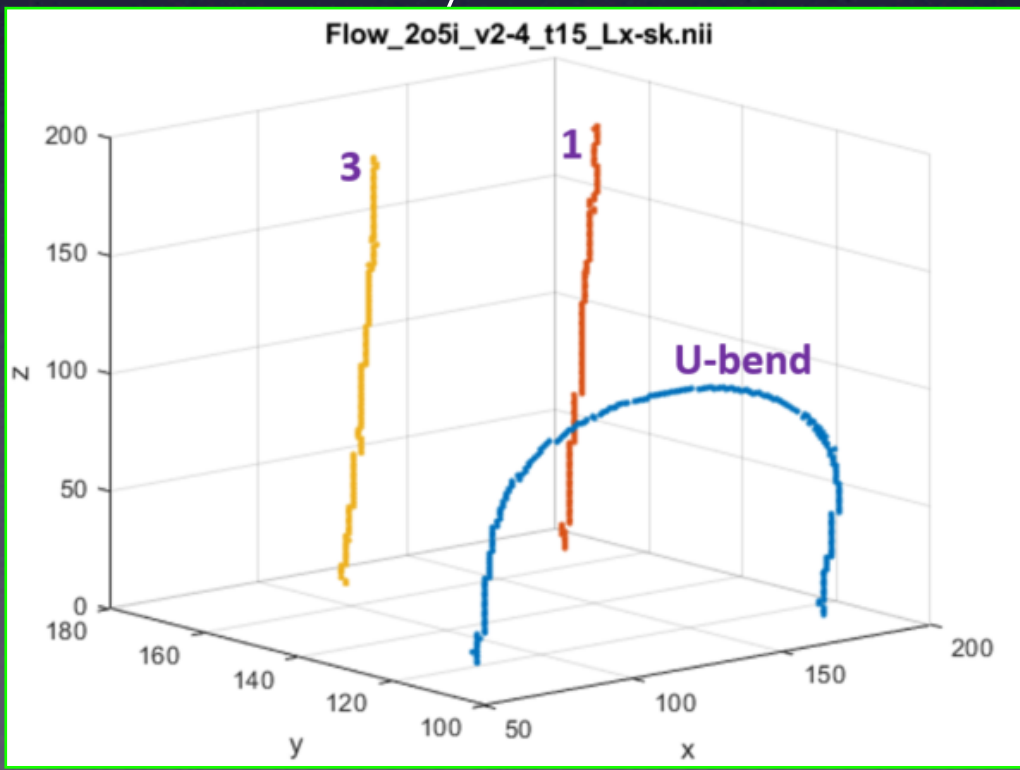


- MR-QA123 Quality Assurance Flow Phantom Set (Shelley)
- CardioFlow 1000 MR pump, 2.5 ml/s
- GE Signa HDxt 1.5 T scanner
- estimated *PSNR* = 30 dB
- voxels: 0.82mm x 0.82mm x 1.01mm

3D segmentation rendering



Binary skeletons





# Results [21]

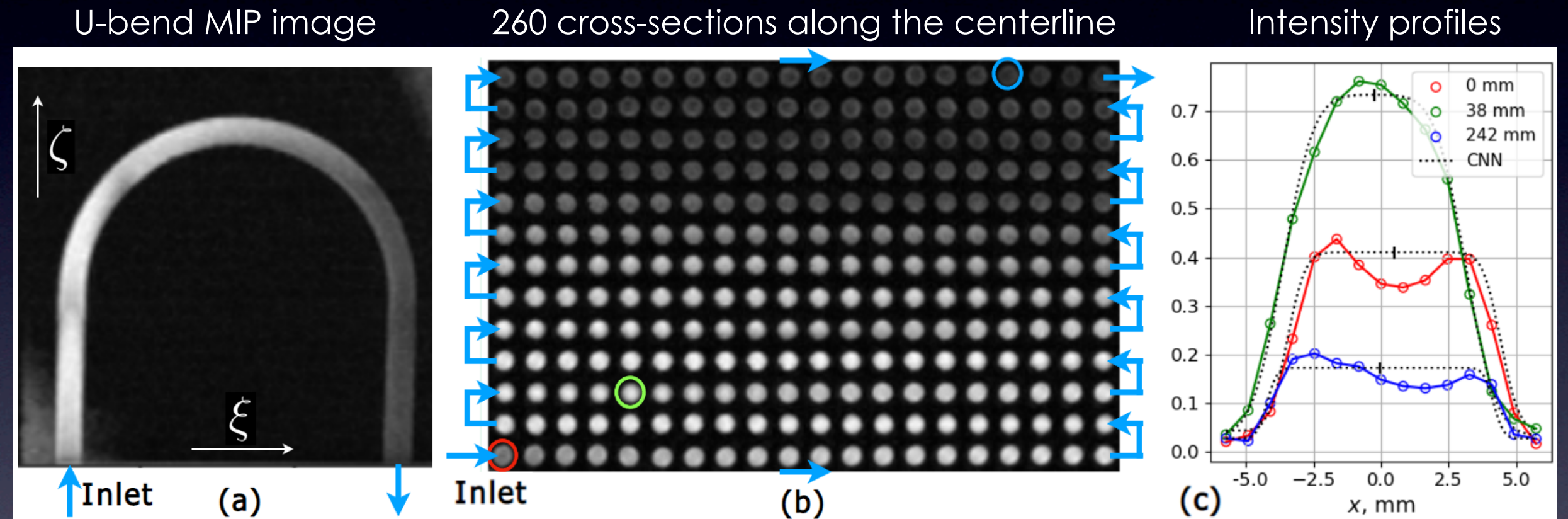
Blood-flow phantom ToF MRA

PC, MS Windows 11  
 16GB RAM, Intel™ i5-8300H CPU @ 2300 MHz  
 NVIDIA GeForce GTX 1050, 4GB GPU  
 Keras and Scipy Python libraries

Image simulation  
 for transfer learning

$$\begin{aligned}
 0 &\leq a \leq 0.3 \\
 0.1 &\leq b \leq 1.1 \\
 1 &\leq R/\Delta_s \leq 6 \\
 0.3 &\leq w/\Delta_s \leq 1.5 \\
 -1.2 &\leq d_x/\Delta_s \leq 1.2 \\
 -1.2 &\leq d_y/\Delta_s \leq 1.2 \\
 \sigma &\approx 0.032
 \end{aligned}$$

$M = 60\,000$  (training set)  
 $M_V = 20\,000$  (validation set)  
 $M_T = 20\,000$  (test set)



- Adam weight  $\phi$  optimization
- ~1 hr of training up to the time of validation error increase, for a single-parameter output and (32,32,32,32,16,8) CNN channels

The sampling interval  
 $\Delta_s = 0.82$  mm

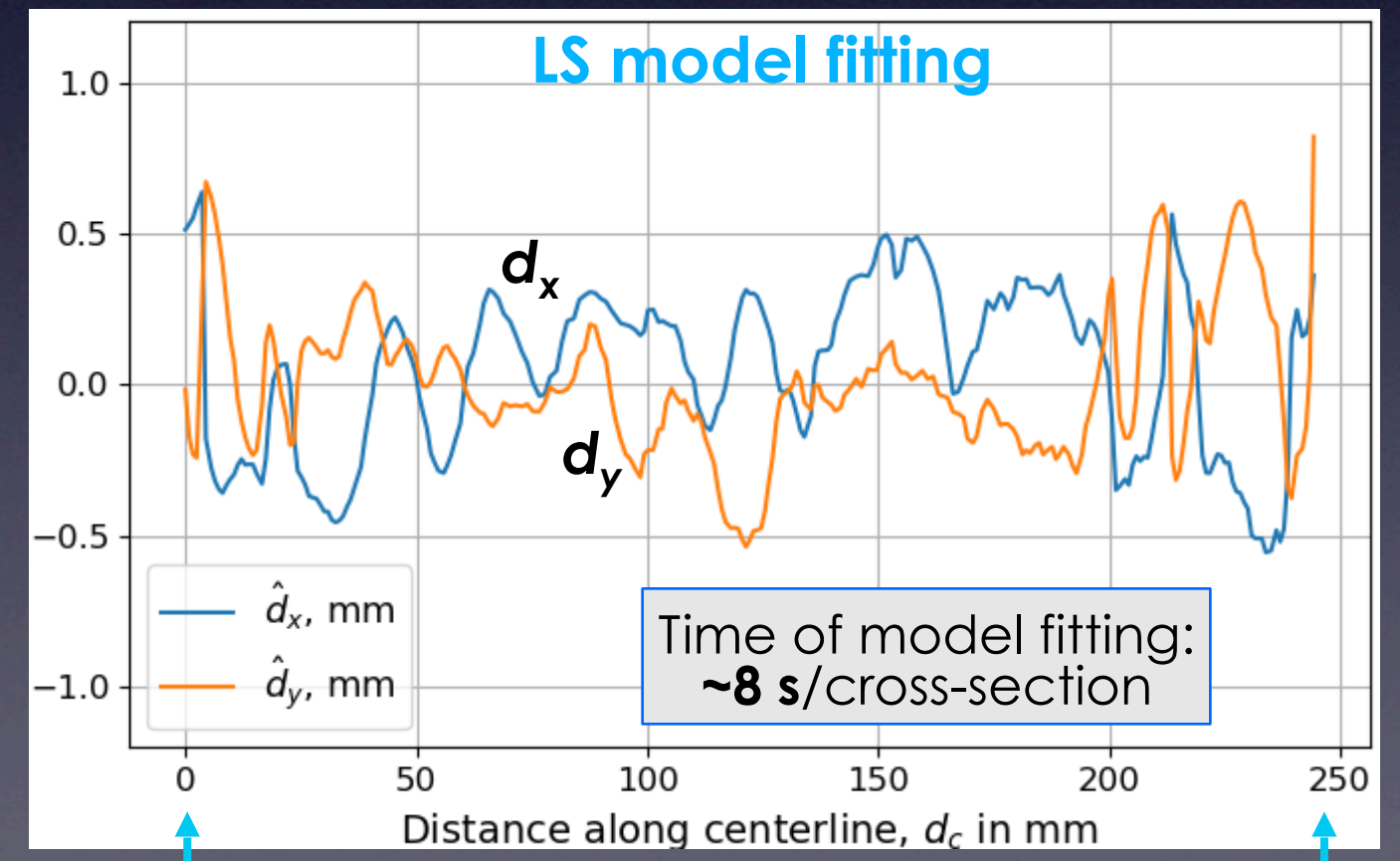
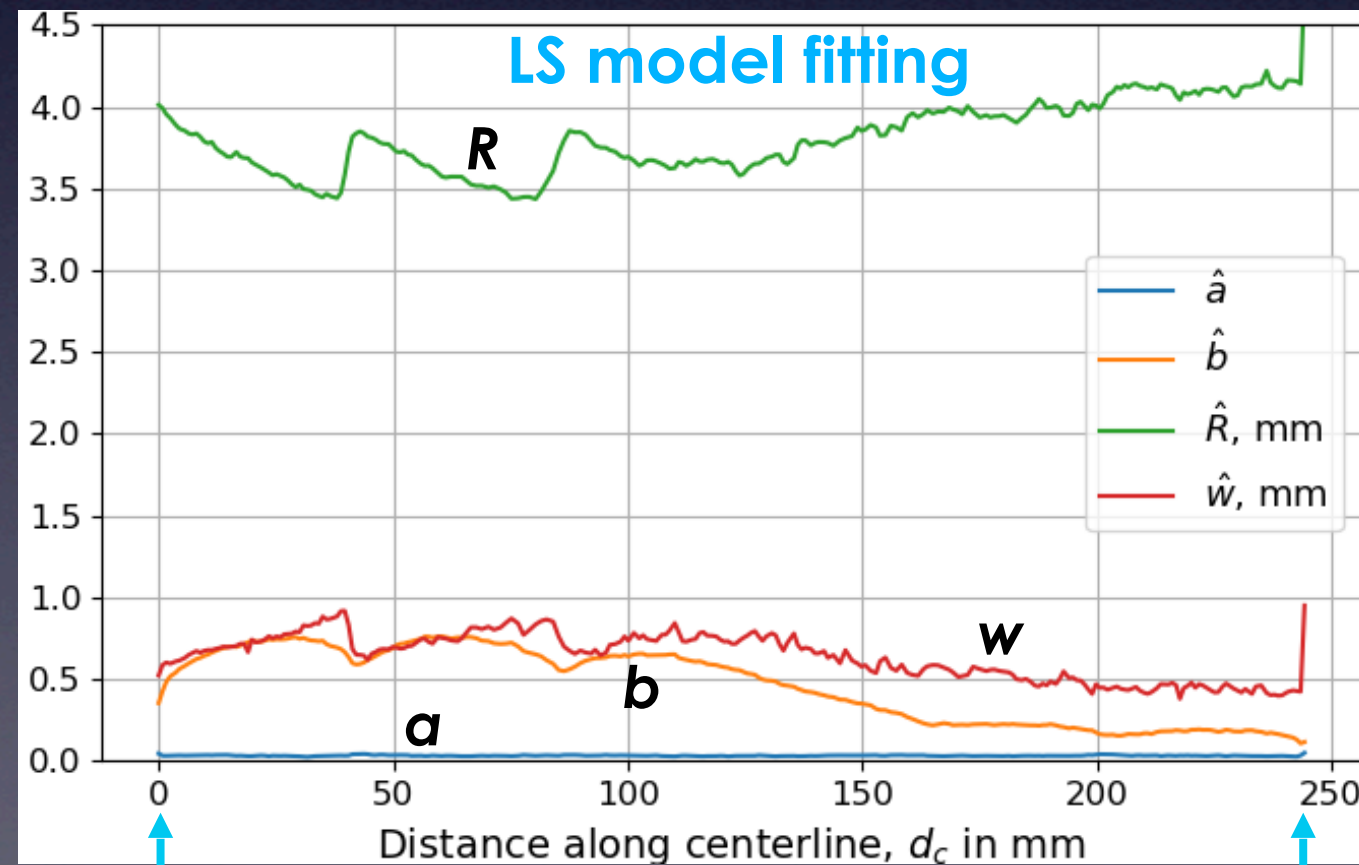
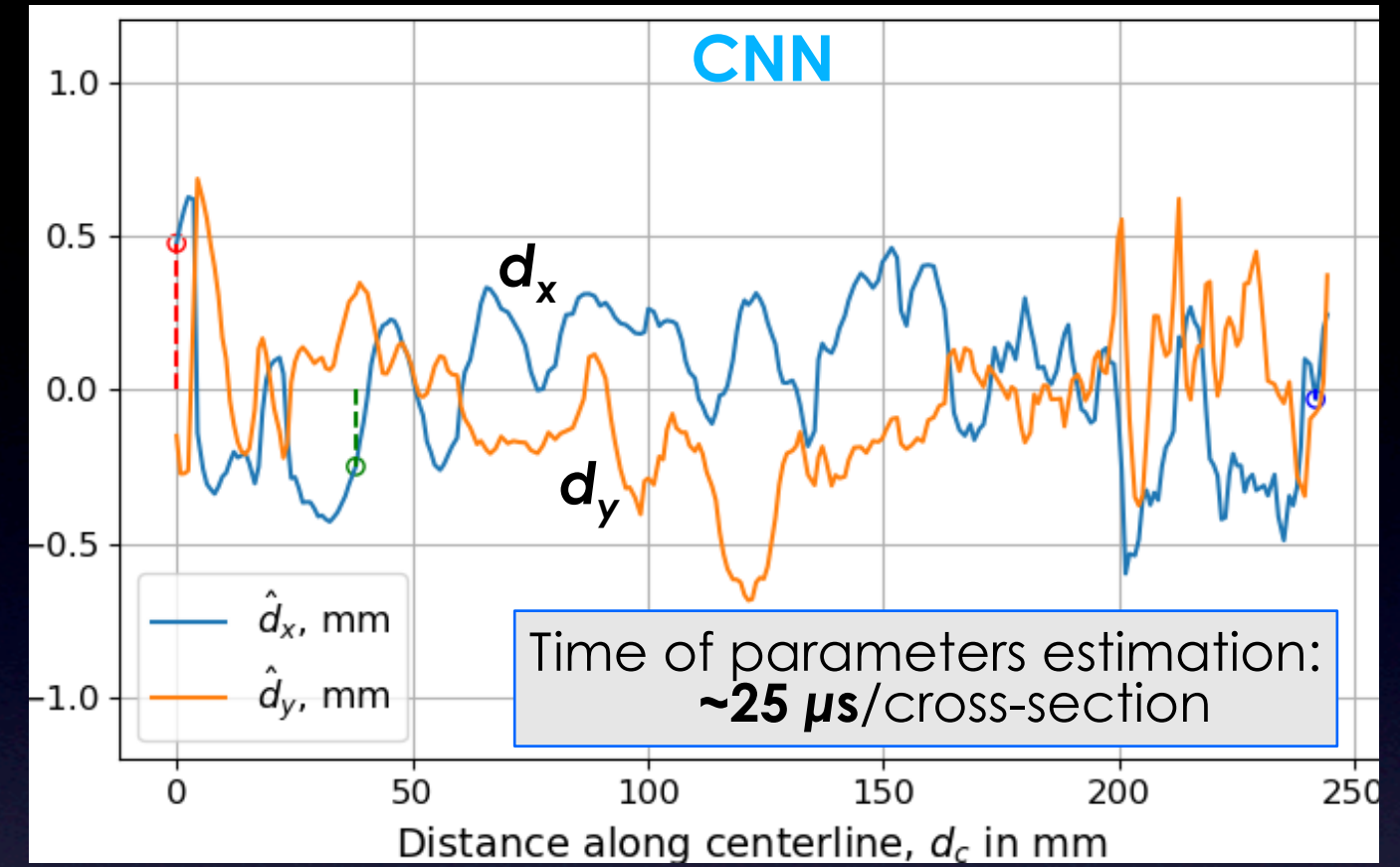
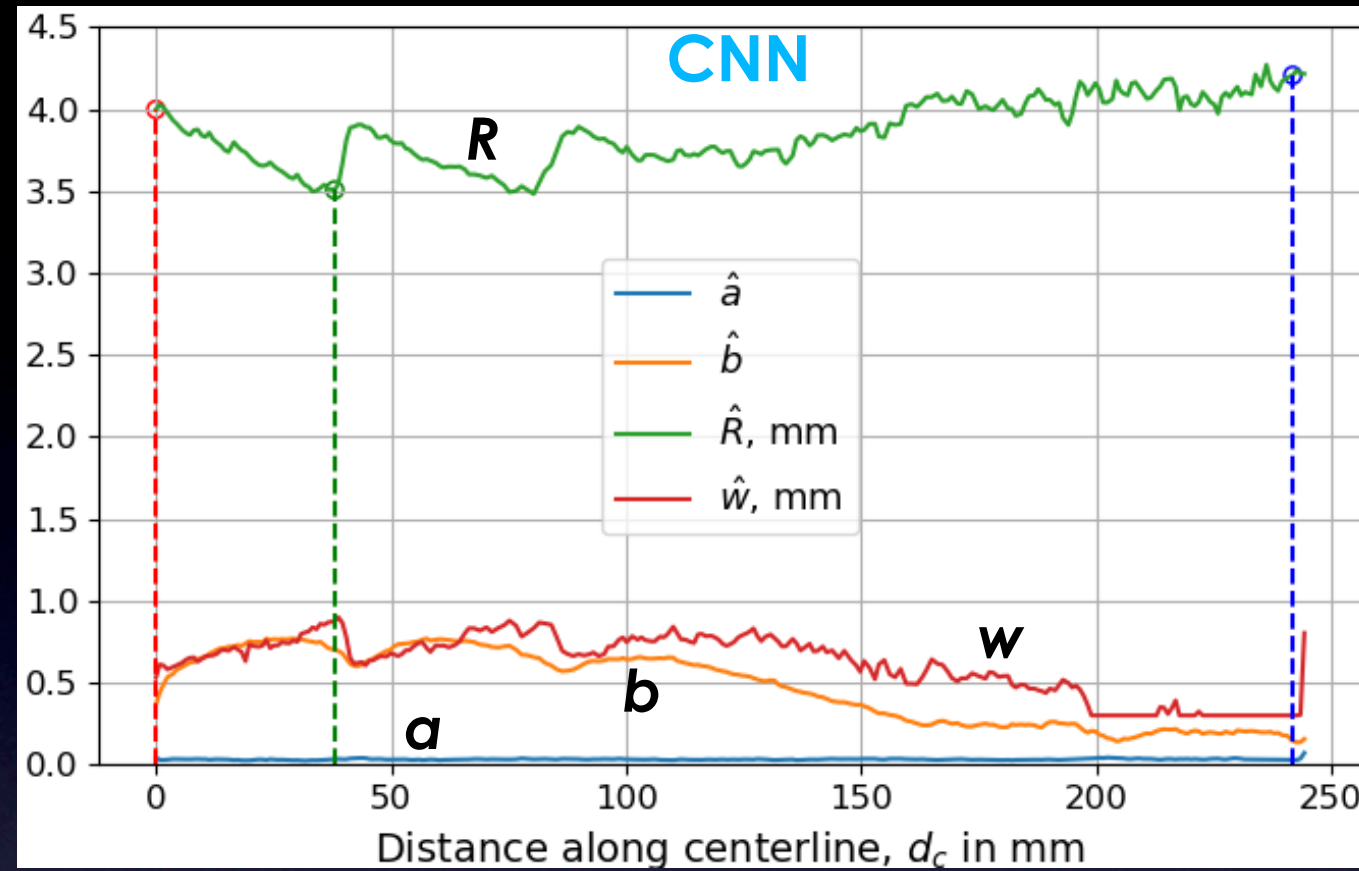


# Results [21]

Blood-flow phantom ToF MRA

## Comparison

- Equally high accuracy
- CNN much faster



The sampling interval  $\Delta_s = 0.82 \text{ mm}$

Inlet

Outlet

Inlet

Outlet



# Example 2

Coronary arteries in CE CTA [4,21]

- Rotterdam Coronary Artery Algorithms Evaluation Framework
- 17 datasets annotated by 3 observers
- voxels of different size: e.g. 0.3mm x 0.3mm x 0.4mm, 0.37mm x 0.37mm x 0.45mm, 0.43mm x 0.43mm x 0.25mm, ...

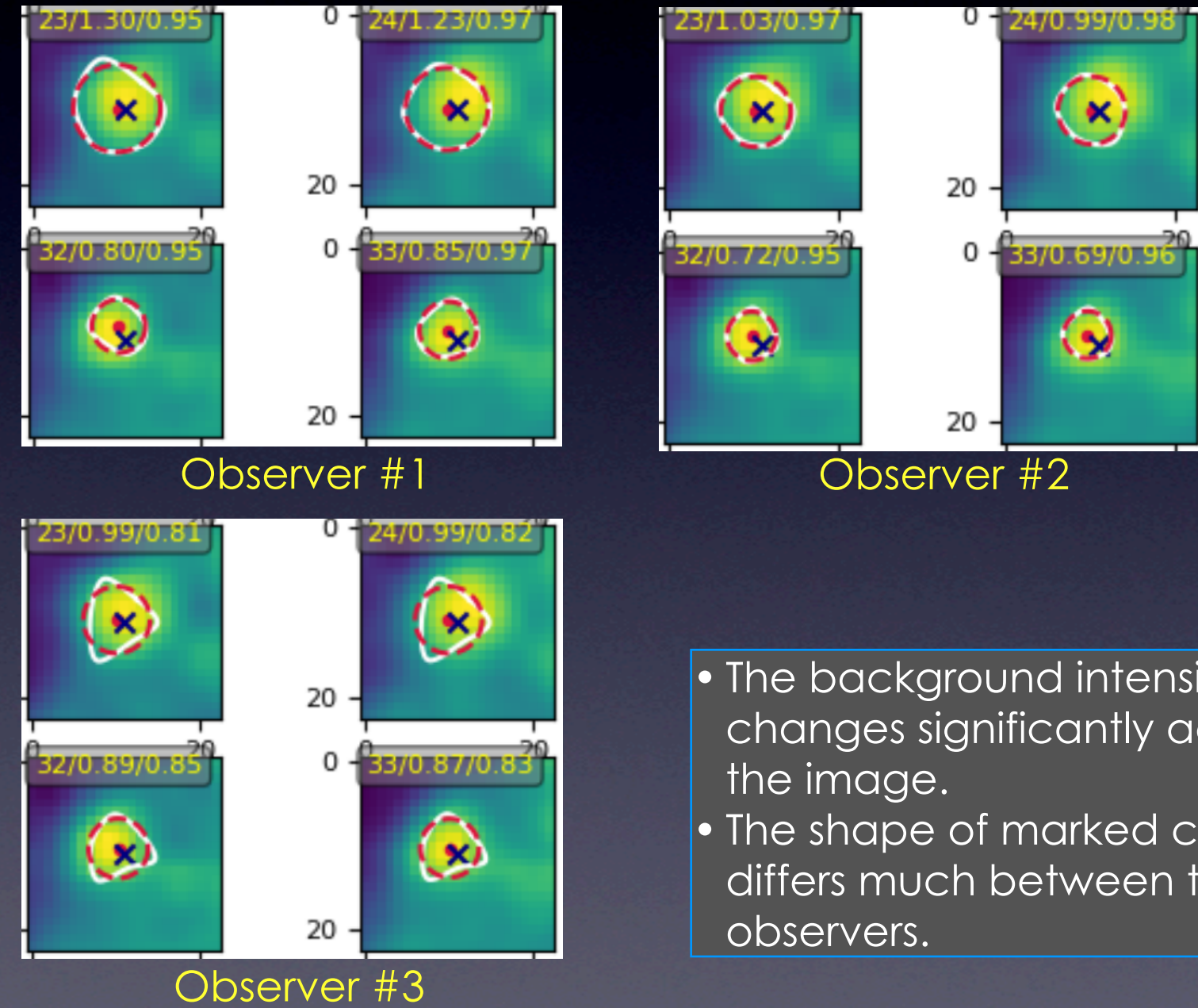
Black cross: centerline intersection point  
 White line: contour marked by observer  
 Red dot: center of mass of the contour  
 Dashed red line: equivalent circle of radius

$$\rho = \sqrt{A/\pi} \quad (3)$$

where  $A$  is the area inside contour.

Values of (3) were substituted for radius  $R$  in (2).

LS model fitting --> errors and excessive computation time.



- The background intensity changes significantly across the image.
- The shape of marked contours differs much between the observers.



# Results [21]

## Equivalent radius of coronary arteries

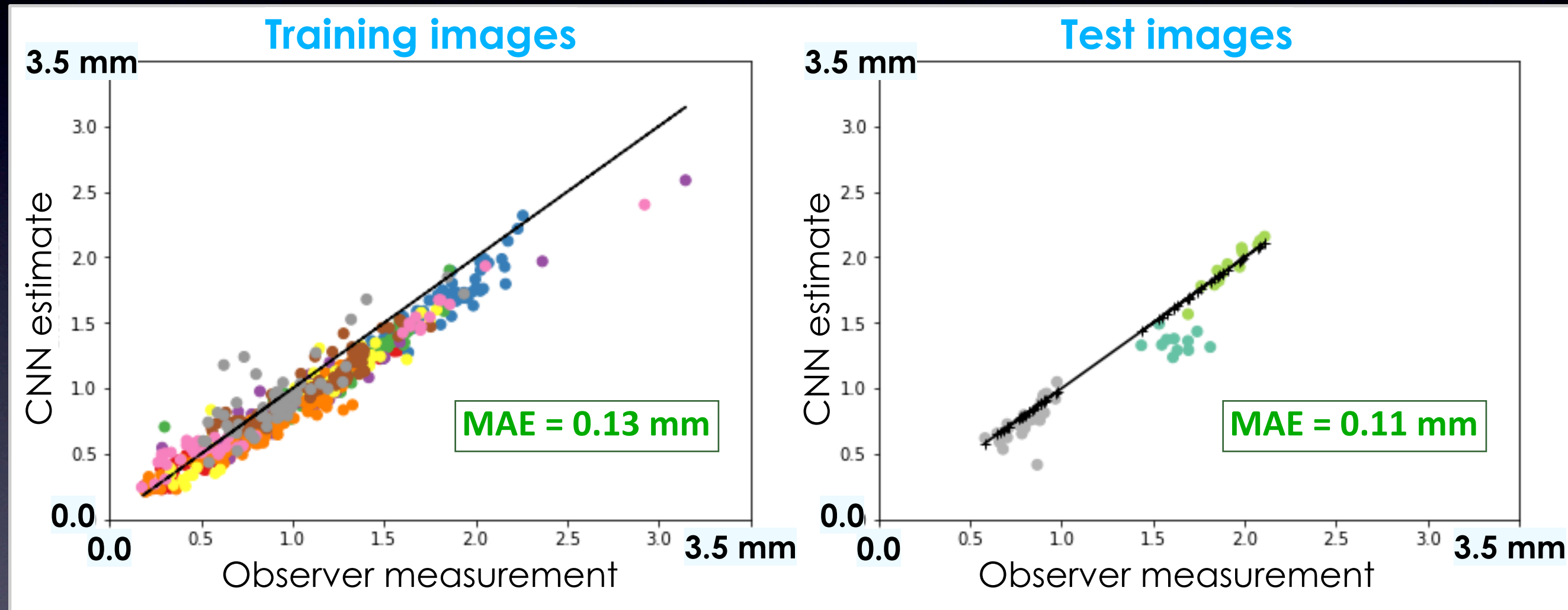
The CNN was trained on real, nonideal images to reduce the estimator sensitivity to spurious objects in the background.

Training set: 558 sections of arteries segments annotated by Observer #1

Test set: 51 sections

The sampling interval  $\Delta_s = 0.45$  mm

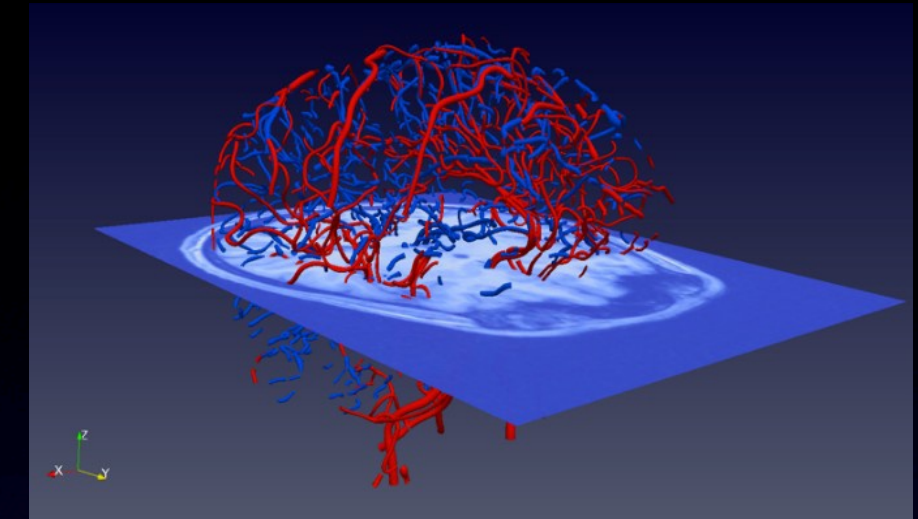
Center of mass shift estimation:  
MAE < 0.09 mm  
(another experiment, not shown here)





## Summary

1. Methods involving binary segmentation fail in performing the thin-branches extraction and quantification tasks.
2. Centerline-based image-formation-model fitting offers subvoxel accuracy, robustness to image nonidealities, and modularity for better processing control.
3. The CNN-based model parameters estimation is promising in terms of speed, accuracy, robustness and flexibility.



## Future research

Automated 3D blood-vessel image processing methods, taking account of

- . vessel centerline tracking [11],
- . anatomical markers detection (e.g. ostia),
- . non-circular cross-sections (e.g. stenoses),
- . denoising,
- . superresolution [20].



# Free software (visualization/segmentation/analysis)

.Multiplatform  
.Interactive



[itksnap.org/](http://itksnap.org/)

University of Pennsylvania

Convert3D

MeshLab

[meshlab.net](http://meshlab.net)

[paraview.org/](http://paraview.org/)  
ParaView

kitware | Glance

[kitware.github.io/glance/](https://kitware.github.io/glance/)

Harvard University

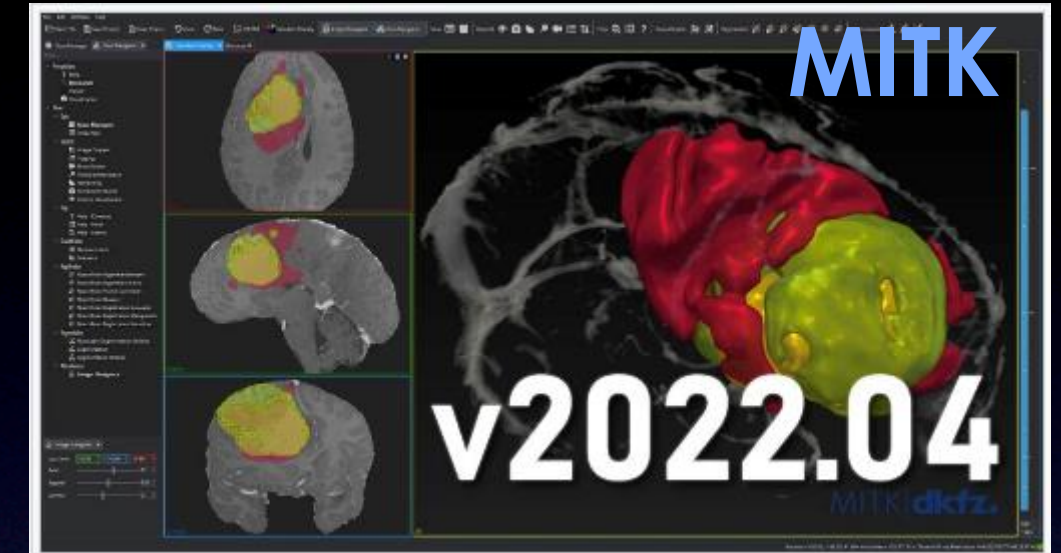
[slicer.org/](http://slicer.org/)



3DSlicer



[simvascular.github.io/](https://simvascular.github.io/)

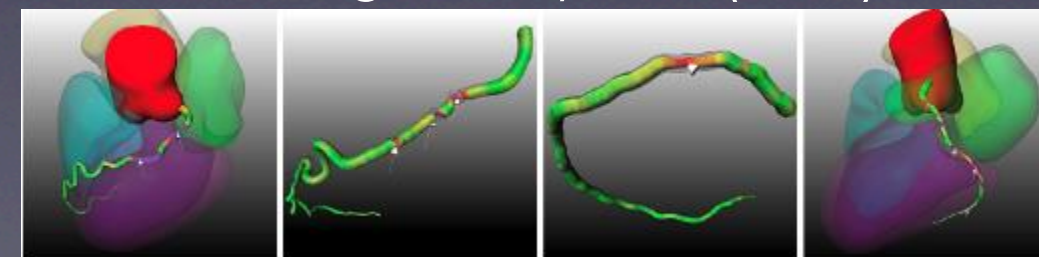


[mitk.org/](http://mitk.org/)

German Cancer Research Center

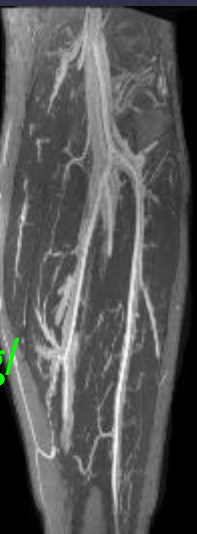
## Blood-vessel image datasets

Kirisli et al.: Standardized evaluation framework for evaluating coronary artery stenosis detection, stenosis quantification and lumen segmentation algorithms in computed tomography angiography, Medical Image Analysis 17 (2013) 859-876



PAVES

<https://paves.grand-challenge.org/>



NITRC NeuroImaging Tools & Resources Collaboratory

<https://www.nitrc.org/projects/icbmmra/>

Magnetic Resonance Angiography Atlas Dataset



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